# חAmIBIA UחIVERSITY <br> OF SCIEMCE AПD TECHחOLOGY <br> FACULTY OF HEALTH AND APPLIED SCIENCES 

DEPARTMENT OF MATHEMATICS AND STATISTICS

| QUALIFICATION: Bachelor of science Honours in Applied Statistics |  |
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| QUALIFICATION CODE: 08BSSH | LEVEL: 8 |
| COURSE CODE: SAT802S | COURSE NAME: SAMPLING THEORY |
| SESSION: NOVEMBER 2019 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| FIRST OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINERS | DR. C.R KIKAWA |
| MODERATOR: | PROF SATHIYA APPUNNI |

## INSTRUCTIONS

1. Answer ALL the questions in the booklet provided.
2. Show clearly all the steps used in the calculations.
3. All written work must be done in blue or black ink and sketches must be done in pencil.

## PERMISSIBLE MATERIALS

1. Non-programmable calculator without a cover.

THIS QUESTION PAPER CONSISTS OF 6 PAGES (including this front page)

# NAMIBIA UNIVERSITY OF SCIENCE AND TECHNOLOGY <br> DEPARTMENT OF MATHEMATICS AND STATISTICS <br> SAMPLING THEORY: SAT802S 

EXAMINATION FIRST OPPORTUNITY, NOVEMBER 2019
Time - 3 Hrs. Attempt all Questions. Maximum marks - 100

## 1. Question

(a) Discuss the following concepts as used in sampling theory, give relevant examples where applicable:
i. Sample survey and census
ii. Pilot survey
iii. Elementary units or elements
(b) Write short notes on the concepts; Probability and Non-probability Sampling.
(c) Discuss why we use or talk about sampling with replacement in sampling theory?
(d) Write short notes on the usage of auxiliary Information with a clear illustration.
(5 marks)
2. Question

The investigator samples 10 one-acre plots by simple random sampling and counts the number of trees (y) on each plot. She also has aerial photographs of the plantation from which she can estimate the number of trees ( x ) on each plot of the entire plantation. Hence, she knows $\mu_{x}=19.7$ and since the two counts are approximately proportional through the origin, she uses a ratio estimate to estimate $\mu_{y}$.

Table 1: To estimate the average number of trees per acre on a 1000- acre plantation

| Plot | Actual no. per acre Y | Aerial estimate X | $y_{i}-r x_{i}$ |
| :---: | :---: | :---: | :---: |
| 1 | 25 | 23 | 0.5625 |
| 2 | 15 | 14 | 0.1250 |
| 3 | 22 | 20 | 0.7500 |
| 4 | 24 | 25 | -2.5625 |
| 5 | 13 | 12 | 0.2500 |
| 6 | 18 | 18 | -1.1250 |
| 7 | 35 | 30 | 3.1250 |
| 8 | 30 | 27 | 1.3125 |
| 9 | 10 | 8 | 1.5000 |
| 10 | 29 | 31 | -3.9375 |
| mean | 22.10 | 20.80 | - |

(a) study Figures 1 and 2 and discuss the suitability of using ratio estimates.


Figure 1: Scatter plot


Figure 2: Regression output
(b) Construct the approximate $95 \%$ confidence interval for $\mu_{y}$

## 3. Question

(a) Discuss the concept a simple random sample in relation to $n$ the sample size and $N$ the population size clearly stating the selection probability of each sample.
(b) Assume you have a population of $N$ elements and you wish to take a sample of $n$ of these elements. Required to state a well known formula from the theory of permutations and combinations which is used to select, the number $T$ of possible samples of $n$ elements from a population of $N$ elements.
(c) Given that a population contains 25 elements and one wishes to take a sample of 5 elements. Use the relation stated in (b) to compute the possible samples of 5 elements from the population given.
(d) Explain, stepwise how to take a Simple Random Sample.
(e) As a researcher you require to use ratio estimates as an estimation method for your analysis, study Figures 1 and 2 in question (2) and discuss the suitability of your meth( $\mathbb{W}$. marks)

## 4. Question

(a) Discuss any three practical cases in which multistage sampling designs are used.
(b) Two-stage sampling includes both one-stage cluster sampling and stratified random sampling as special cases.

1. When does two-stage sampling reduce to cluster sampling?
2. When does two-stage sampling reduce to stratified random sampling?
(c) There are 36 departments in a small liberal arts college. One wants to estimate the average amount of money the students spent on textbooks last semester. Since the size of each department varies very much, a two-stage cluster sampling using probability proportional to size for the primary unit is carried out. The results are listed in the table below. Estimate the population mean using probability proportional to size estimator (Hansen-Hurwitz) and estimate the variance of that estimator.

| Department | $M_{i}$ | $m_{i}$ | Textbook expenses in S for last semester |
| :--- | :---: | :--- | :--- |
| 1 | 10 | 4 | $326,400,423,443$ |
| 2 | 20 | $S$ | $275,312,450,350.227,438,512,403$ |
| 3 | 30 | 12 | $512,256,332,402.512,309,411,610,422,630.550,470$ |
| 4 | 15 | 6 | $426,312,512,440.342 .533$ |

Figure 3: Table of values
5. Question
(a) Discuss the concept, double sampling clearly stating its major advantages.
(b) A forest resource manager is interested in estimating the total number of dead trees in a 400 acre area of heavy infestation. She subdivides the area into 200 plots of equal sizes and uses photo counts to find the number of dead trees in 18 randomly sampled plots. She then randomly samples 8 plots out of these 18 plots and conducts a ground count on these 8 plots.
Note: Study the tables and output given for the estimation of the total number of dead trees in the 400 acre area. So as to answer the questions that follow.

Let $x$ denote the number of dead trees in the plot by photo count and $y$ the number of dead trees by ground count. The data are given as:

| Plot | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $x^{\prime}$ | 5 | 7 | 10 | 6 | 7 | 9 | 3 | 6 | 8 | 11 | 5 | 9 | 12 | 13 | 3 | 20 | 15 | 4 |

Ont of these is plots, 8 are randomly selected and a ground count is conducted.

| Plot | 2 | 3 | 5 | 6 | 12 | 15 | 16 | 17 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $x$ | 7 | 10 | 7 | 9 | 9 | 3 | 20 | 15 |
| $y$ | 9 | 13 | 10 | 11 | 10 | 4 | 25 | 17 |
| $y-x x$ | 0.3375 | 0.6250 | 1.3375 | -0.1375 | -1.1375 | 0.2875 | 0.2500 | -1.5625 |


| Variable | N | Mean | StDev |
| :---: | :---: | :---: | :---: |
| 8' | 18 | 8.50 | 4.48 |
| x | 8 | 10.00 | 5.2e |
| Y | E | 12.37 | e. 28 |
| Sum of $x^{\prime}=153.00$, Sun of $x=80.00$.Sum of ${ }^{\text {a }}$, |  |  |  |
|  |  |  |  |

Figure 4: Tables of values and output
i. Compute the ratio estimate for the population total.
ii. compute the estimated variance of the ratio estimator: use the following quantities where applicable

$$
\begin{aligned}
& s^{2}=(s t . d e v \cdot y)^{2}=6.28^{2} \\
& \sum_{i=1}^{8}\left(y_{i}-r \cdot x_{i}\right)^{2}=6.1928
\end{aligned}
$$

## END

